ANGLE PAIRS & PROOFS Mastery Check

 $\overline{EH}$  and  $\overline{HK}$  represent two perpendicular mirrors.  $\overline{DF}$  and  $\overline{CG}$  show two parallel light rays that reflect off the mirrors so that  $\overline{DF} \parallel \overline{CG} \parallel \overline{IB} \parallel \overline{JA}$  and  $\overline{FJ} \parallel \overline{GI}$ . When light reflects, the angle of reflection is congruent to the angle at which the light strikes the surface. For example,  $\angle EFD \cong \angle GFM$ .



- 1. What postulate, property, or theorem tells us that EF + FG = EG?
- 2. Name a postulate and a property that together justify saying that if  $m \angle EFD = m \angle GFM$ , then  $m \angle EFM = m \angle GFD$ .
- 3. Write the Linear-Pair Postulate using  $\angle FMC$
- 4. We know that  $\overrightarrow{CM} \parallel \overrightarrow{BL}$ , but how do we know that there is not some other line parallel to  $\overrightarrow{BL}$  that goes through point *M*?
- 5. What postulate would allow us to construct a line through *A* and *G* and know that there are no other possible lines that pass through these two points?
- 6. What postulate, property, or theorem tells us that  $\angle FMC \cong \angle LJA$ ?
- 7. (a) If  $m \angle CML = 145^\circ$ , what is  $m \angle AJM$ ? (b) What theorem allowed you to figure that out?
- 8. If  $m \angle MLB = 32^\circ$ , what is  $m \angle GIH$ ?
- 9. If  $m \angle CML = 8x 5$  and  $m \angle ILM = 6x + 32$ , what is  $m \angle LJA$ ?

10. Two parallel lines are intersected by a transversal. A pair of same-side-interior angles measure  $18x - 2y^{\circ}$  and  $2x + 6y^{\circ}$ . A pair of alternate-exterior angles measure  $9y + 1^{\circ}$  and  $5x + 6^{\circ}$ . Find the values of x and y.

11. Two parallel lines are intersected by a transversal. A pair of corresponding angles measure  $x^2 - 2x - 6^\circ$  and  $8x + 18^\circ$ . What are the measures of the angles in degrees?

**Given:** Lines are parallel as shown. **Prove:**  $m \angle 1 = m \angle 5$ **Directions:** Fill in the reasons to justify each of the statements

60	
1º	
e statements	
	7

Statement	REASON
Lines are parallel as shown.	given
$m \angle 1 + m \angle 2 = 180^{\circ}$	12.
$m \angle 2 = m \angle 3$ and $m \angle 3 = m \angle 4$	13.
$m \angle 2 = m \angle 4$	14.
$m \angle 1 + m \angle 4 = 180^{\circ}$	15.
$m \angle 5 + m \angle 4 = 180^{\circ}$	16.
$m\angle 1 + m\angle 4 = m\angle 5 + m\angle 4$	17.
$\therefore \qquad m \angle 1 = m \angle 5$	18.





- 1. If  $\angle ICD \cong \angle HDE$ , what postulate allows us to say that  $\overline{IC} \parallel \overline{HD}$ ?
- 2. If AB = CD, what property tells us that AB + BC = BC + CD?
- 3. What postulate allows us to conclude in the previous problem that AC = BD?
- 4. What postulate allows us to write  $m \angle HDG + m \angle GDE = \angle HDE$ ?
- 5. If  $m \angle HDE = m \angle ICD$  and  $m \angle GDE = m \angle HCD$ , why does  $m \angle HDE m \angle GDE = m \angle ICD m \angle HCD$ ?
- 6. If  $\overrightarrow{FE} \perp \overrightarrow{AE}$ , how can we be sure that there is not some other line through F that is perpendicular to  $\overrightarrow{AE}$ ?
- 7. If 3(AB + AC) = 72, what property allows us to write AB + BC = 24?
- 8. Write the Linear-Pair Postulate using  $\angle HDC$ .
- 9. How do you know that  $\overline{HD} \cong \overline{HD}$ ?
- 10. If  $m \angle AIB + m \angle BIC + m \angle CIH = 115^{\circ}$  and  $m \angle DGE = \angle BIC$ , how do we know that  $m \angle AIB + m \angle DGE + m \angle CIH = 115^{\circ}$ ?